

Lattice Expansion in Hybrid Perovskites: Effect on Optoelectronic Properties and Charge Carrier Dynamics

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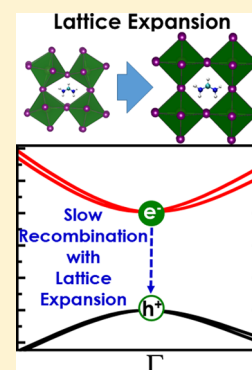
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Supporting Information

ABSTRACT: Hybrid halide perovskites frequently undergo structural expansion due to various stimuli, significantly affecting their electronic properties and in particular their charge carrier dynamics. It is essential to atomistically model how geometric changes modify electronic characteristics that are important for applications such as light harvesting and lighting. Using *ab initio* simulations, here we investigate the structural dynamics and optoelectronic properties of FAPbI₃ under tensile strain. The applied strain leads to elongation of the Pb–I bonds and a decrease in the level of PbI₆ octahedral tilting, which manifests as blue-shifts in band gaps. Nonadiabatic molecular dynamics simulations further reveal that charge carrier recombination rates moderately decrease in these expanded lattices. The complex influence of lattice dynamics on electron–phonon scattering results in a longer carrier lifetime, which is advantageous for efficient solar cells. By providing detailed information about the structure–property relationships, this work emphasizes the role of controlled lattice expansion in enhancing the electronic functionalities of hybrid perovskites.



Organic–inorganic hybrid perovskites have emerged as one of the most promising candidates for new-generation light harvesters in photovoltaic devices, photo-detectors, and light-emitting diodes.^{1–8} The coalescence of many desirable properties such as a long carrier diffusion length, strong visible light absorption, a widely tunable optical band gap, and insensitivity to defects has made halide perovskites highly suitable for many optoelectronic technologies.^{9–11} Most studied three-dimensional hybrid lead iodide perovskites have an APbI₃ structure, where corner-sharing PbI₆ octahedra form a cuboctahedral cage in which the monovalent organic A cation [e.g., methylammonium CH₃NH₃⁺ (MA⁺) or formamidinium CH(NH₂)₂⁺ (FA⁺)] resides. Due to the mechanical softness of hybrid perovskites, external influences and elemental/molecular size mismatch during compositional engineering give rise to structural distortions.^{12–17} The latter considerably influences the long-term stability and performance of perovskite-based devices. Consequently, controlled lattice distortion has been demonstrated as a powerful tool for tuning and optimizing the optoelectronic properties of halide perovskites.^{16,18–20} In this regard, improved performances have been reported recently for expanded lattices of these materials.^{19–23} Approaches such as mixing large A cations or

continuous light illumination of crystals have been applied to precisely control the lattice expansion. As a result, the emerging improved crystallinity, better band alignment with charge-collecting layers, suppressed nonradiative recombination, and longer carrier diffusion all cumulatively boost the photovoltaic efficiencies of these materials. It should also be noted that hybrid perovskite thin films remain under residual strain, which originates from the compositional inhomogeneity and polycrystallinity of the samples.^{24–27} Combining several diffraction and microscopy techniques, recent studies have identified the presence of significant tensile strain in mixed (MA/FA) and single (MA) cation perovskites films.²⁶ This intrinsic residual strain has been suggested to be the reason for largely heterogeneous photoluminescence and restricted charge dynamics in thin films.^{28–31} Despite those developments, the effect of tensile strain on the optoelectronic functionalities of halide perovskites has yet to be explored and understood at an atomistic level.

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In recent studies, we have explored the polaron formation, structural dimensionality reduction, and compositional engineering of halide perovskites.^{14,32–38} In the work presented here, we use *ab initio* simulations to investigate the structural evolution of FAPbI₃ under tensile strain and its influence on the optoelectronic properties and charge carrier dynamics. We demonstrate that lattice expansion elongates the Pb–I bonds and decreases the level of PbI₆ tilting. These structural changes increase the band gap by decreasing the energy of the valence band edge. This calls for the use of hole-collecting layers with proper energetic band alignment to improve interfacial charge transport. Lattice dynamics exhibit enhanced structural fluctuations in these expanded lattices. Nonadiabatic molecular dynamics (NAMD) simulations further demonstrate that the electron–hole recombination time increases for FAPbI₃ under tensile strain. A combination of several factors such as a reduced level of nonadiabatic electron–phonon coupling, quicker decoherence between the participating states, and a blue-shifted band gap results in a slightly longer carrier lifetime, which is beneficial for optoelectronics. Our study concludes that controlled lattice expansion of halide perovskites is a promising route for enhancing device performances.

We start our simulations by investigating the structural response of FAPbI₃ under mechanical tensile strain. Initially, two structural models that correspond to the tetragonally distorted low-symmetry orthorhombic phase and the high-symmetry cubic phase were considered. These two structures notably differ by the extent of PbI₆ octahedral tilting (see Figure S1a,b). Optimizing both structures at 0 K, without any constraints or applied tensile strain, we find that the orthorhombic crystal is more stable than the cubic one (Figure S1c). Moreover, to include the finite temperature effects, we performed *ab initio* molecular dynamics (AIMD) simulations on orthorhombic FAPbI₃ at 300 K. As shown in Figure S2a, the time-averaged structure is relatively more symmetric with less tilted PbI₆ octahedra. Nevertheless, we find significant symmetry lowering octahedral tilting in the lattice across the instantaneous geometries (Figure S2b). These differences in time-averaged and instantaneous structures agree well with previous experimental and computational studies.^{39–41} X-ray diffraction (XRD)-based measurements that provide time-averaged structures with long coherence lengths reported a high-symmetry cubic phase of FAPbI₃ at room temperature.⁴² However, high isotropic atomic displacement parameters obtained from a neutron diffraction study indicate the presence of considerable octahedral tilting and local distortion in this halide perovskite.⁴³

Under lattice expansion, the relative energy difference between the orthorhombic and cubic phases remains almost unchanged (Figure S3), suggesting the former as the ground state phase. Note that recent studies have reported the appearance of a cubic phase with lattice expansion,^{20,22} however, our results demonstrate that the local geometry remains distorted with low symmetry under tensile strain. Thus, we investigate the effect of lattice expansion only in the orthorhombic phase.

As shown in Figure 1a and Figure S4a, under isotropic tensile strain, the volume of FAPbI₃ increases, expanding all of the lattice parameters. The relative volume expansion in our computational model is within the range reported for the experimental studies based on dimethylammonium (DMA) and guanidinium (GA) mixed perovskites, MA_{1-x}DMA_xPbI₃ and MA_{1-x}GA_xPbI₃ ($x \leq 0.25$) (see Figure S5).^{21,22} The Pb–I

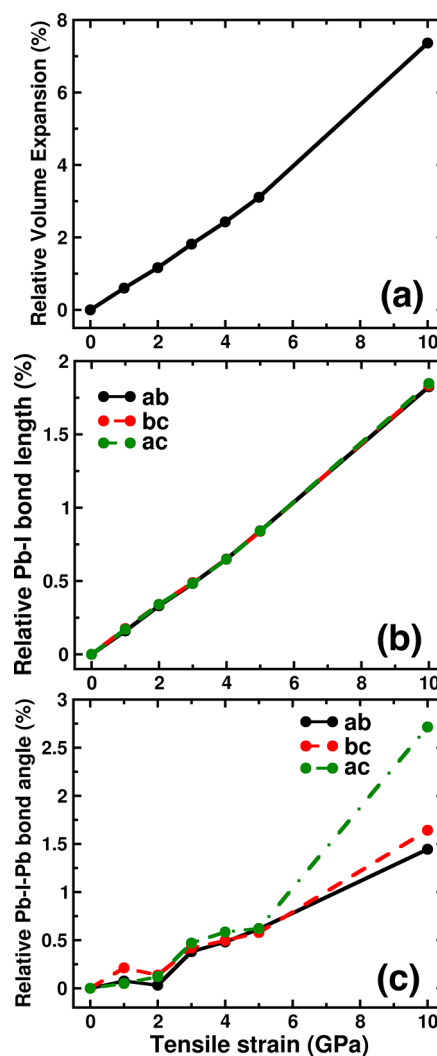


Figure 1. Effect of lattice expansion on the structure of FAPbI₃. Relative changes in (a) lattice volume, (b) averaged Pb–I bond length, and (c) Pb–I–Pb angle averaged over three Cartesian planes. The corresponding absolute values are shown in panels a–c of Figure S4, respectively.

bond lengths increase in all spatial directions relatively equally, revealing the isotropic nature of the cell expansion (Figure 1b and Figure S4b). Note that a slightly longer Pb–I bond [0.01 Å (Figure S4b)] along the *a*–*b* plane indicates a small tetragonal distortion in the lattice. In addition, as shown in Figure 1c and Figure S4c, the average Pb–I–Pb bond angles along all crystal planes increase with lattice expansion, demonstrating a reduced level of PbI₆ octahedral tilting. Thus, an isotropic tensile strain pushes the entire lattice toward a more symmetric phase as also found in experiment.^{19,20,22} However, unlike experimental reports, we did not find any phase transition within the range of applied strain. As mentioned above, this disagreement can arise from the fact that XRD-based experiments poorly capture short time-scale local geometric distortions. Thus, the reported experimental high-symmetry phase can always have a locally distorted low-symmetry structure that our computational study finds as the ground state geometry.

We next explore the effect of tensile strain on the optoelectronic properties of FAPbI₃. It is well established that even though semilocal exchange-correlation functionals

can accurately predict the ground state structures of these materials, calculated electronic properties using this level of theory deviate significantly from experimental reports.^{11,44}

Thus, to correctly simulate the band gap and band edge energies, we include both spin–orbit coupling (SOC) and range-separated hybrid exchange–correlation functionals (HSE06 with a tuned α parameter) in our simulations (see [Methods](#)). The band gap, as shown in [Figure 2a](#), shifts to larger

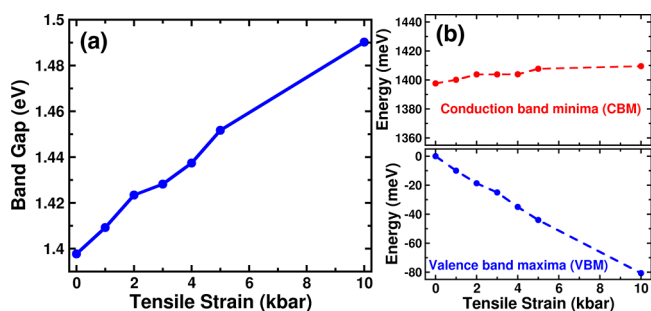


Figure 2. Modification of the electronic properties of FAPbI₃ under tensile strain calculated using the HSE06+SOC approach. (a) Blue-shift of the band gap. (b) Energy shift for conduction band minima (CBM, top) and valence band maxima (VBM, bottom). Plotted energies are scaled to the VBM of pristine FAPbI₃.

values with enhanced lattice strain, suggesting a blue-shift in the optical absorption spectra. In addition, plotted band structures in [Figure S6](#) exhibit the direct band gap nature of FAPbI₃ at the Γ point with or without lattice expansion. This tensile strain-induced band gap increase is quite consistent with the experimental reports in which the lattice expands due to incorporation of large A cations such as GA, DMA, and ethylammonium (EA) ions.^{20–23} Note that the effect of strain on the band gap is much smaller than the other tuning approaches such as halide substitution or B metal alloying that change the gap by hundreds to thousands of millielectronvolts.^{33,45–47} This suggests lattice strain is a promising tool for fine-tuning the band gap that is strongly desired for hybrid perovskite-based tandem solar cells.^{48–50}

The energetic alignments between the frontier bands of halide perovskites and charge transport layers are very crucial for device performance.^{51–33} Recently, several studies have indicated that the band alignment is very sensitive to the residual strain present in the perovskite absorber layer.^{17,19,26} To model variations in the band edge energies of FAPbI₃ under different tensile strains, we aligned all of the bands with

respect to a deep state level (see [section S1 of the Supporting Information](#) for details).^{14,54,55} As shown in [Figure 2b](#) (bottom panel), the band edges are sensitive to applied tensile strain. In particular, the energy of the VBM continuously decreases, whereas that of the CBM remains almost unaffected with a slight upshift in response to increased lattice strain. These computational results are in excellent agreement with a recent experimental study based on the combined techniques of electrochemical impedance spectroscopy and transient photovoltage decay measurements.²⁶ Note that, as discussed in a recent study, the relative band edge positions of low-dimensional halide perovskites can be modified differently under applied strain.⁵⁶

To understand the atomistic reasons for these modified optoelectronic properties, we scrutinized the changes in the electronic nature of FAPbI₃ band edges under lattice expansion. The antibonding overlap between Pb (6s) and I (5p) orbitals forms the VB, whereas Pb 6p orbitals predominantly form the CB with a small contribution from I (5p), making the band a largely nonbonded state (see [Figure S7](#) for electronic charge density plots of the VBM and CBM). We further analyzed the crystal orbital Hamilton population (COHP) of these band edges to assess the influence of lattice expansion on these states. The COHP calculates partitioned orbital-pair interactions, that is, the bond-weighted density of states between a pair of neighboring atoms, and its integrated value (ICOHP) provides the bond strength.^{57,58} The details of this population analysis can be found in [section S2](#). As shown in [Figure 3a](#), a negative ICOHP value for the valence band, including the Pb 6s and I 5p orbitals, indicates its antibonding character as also found from charge density analysis ([Figure S7](#)). Moreover, the ICOHP value for the VB decreases with tensile strain. In contrast, the ICOHP values for the conduction band are much smaller, reconfirming its nonbonding character (see [section S2](#) and [Figure S8](#)). As the PbI cages expand through elongation of the Pb–I bonds, the antibonding overlap between Pb 6s and I 5p orbitals in the VB decreases. The reduced level of antibonding in the VBM further shifts its energy level downward as shown in [Figure 2b](#) (bottom panel). However, due to its dominant nonbonding orbital overlap, the CB does not change significantly under lattice expansion. Because the CBM level is mostly unchanged, the band gap increases with lattice expansion. Notably, the octahedral tilting of PbI₆ decreases with lattice expansion. This results in more linear Pb–I–Pb angles ([Figure 1c](#)), which enhances the antibonding overlap in the VBM. However, changes in the Pb–I bond distances dominate versus changes

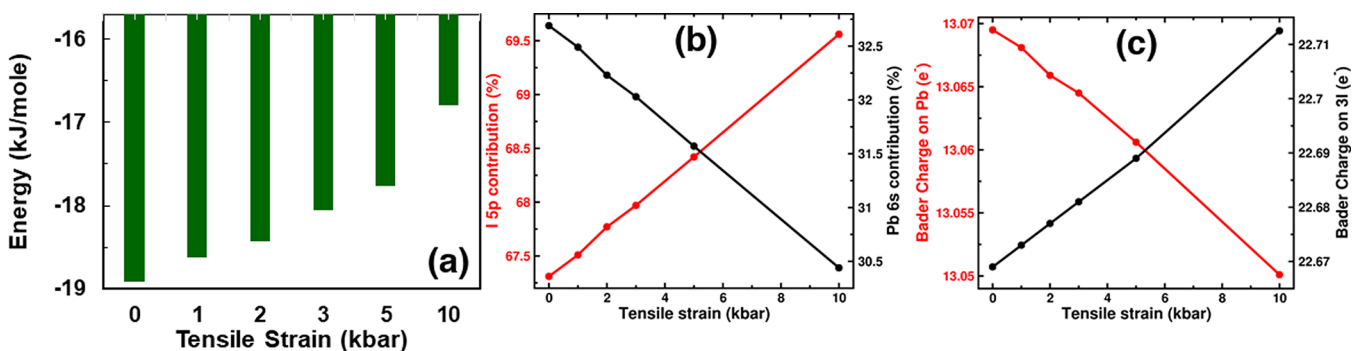


Figure 3. Effect of tensile strain on the band edges and charge distribution in FAPbI₃. (a) Integrated COHPs depicting the antibonding strength at the VBM. (b) Relative contribution of I 5p and Pb 6s orbitals to the VBM. (c) Bader charges on Pb and I atoms per formula unit of FAPbI₃.

in the Pb–I–Pb angles in influencing the orbital overlap and relative energy position of the VBM.

We additionally analyzed the change in relative orbital contributions to the band edges with lattice expansion. As plotted in Figure 3b, the I (5p) increases whereas Pb (6s) decreases their contribution to VBM. This consequently indicates an enhanced ionic character of this state with a localized charge density on iodide atoms. The contributions of Pb (6p) orbitals to the CBM increase with lattice expansion, although to a lesser extent compared to the respective effect in the VBM (see Figure S9). The calculated atomic Bader charges as plotted in Figure 3c further demonstrate that with lattice expansion, more electrons accumulate on iodide atoms and the lead atoms become more positively charged. This trend in charge redistribution confirms the enhanced ionicity of the Pb–I framework of FAPbI₃ subject to tensile strain.

Thus, lattice expansion in FAPbI₃ tends to localize the VBM charge density over iodide anions, making the inorganic framework chemically more ionic. However, the CBM remains essentially unaffected by the tensile strain.

The low bulk modulus of the hybrid perovskite lattice gives rise to structural fluctuations even under ambient conditions.^{32,59,60} Recent studies demonstrate that such fluctuations significantly influence the photogenerated charge carrier dynamics in these materials.^{60–64} We therefore explore the changes in structural motions upon lattice expansion and the effect on carrier dynamics in FAPbI₃ by using AIMD (see Methods). Note that, due to large structural fluctuations at high tensile strains, we restrict the MD simulations of FAPbI₃ to run under 5 kbar expansive pressure.

In particular, we focus on the dynamics of the PbI framework as it is dominant in accommodating the charge carriers in halide perovskites (see Figure S7). The calculated root-mean-square fluctuations (RMSFs) for Pb and I atoms of FAPbI₃ under different tensile strain are shown in Figure 4a.

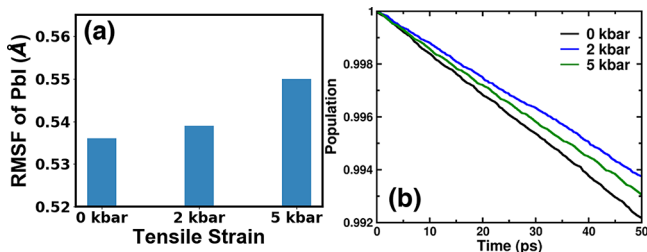


Figure 4. (a) Effect of lattice expansion on lattice dynamics. The root-mean-square fluctuation for PbI at 300 K shows more dynamical behavior under tensile strain. (b) Charge carrier recombination in FAPbI₃ under tensile strain. Partial suppression of nonradiative recombination of photogenerated electrons and holes in an expanded lattice.

With the lattice expansion, the RMSFs imply that the number of spatial fluctuations of the PbI frame increases. As the lattice volume increases, the PbI₆ octahedron accesses more space to mutually distort the cage geometry, resulting in a more rotationally disordered structure.

NAMD-based simulations have been performed to link the effect of lattice expansion to the charge carrier dynamics in FAPbI₃. To determine the effect of the tensile strain on the nonradiative electron–hole recombination rate, we compute the time-dependent population of the first excited state that has been modeled by exciting an electron from the VBM to the

CBM at the Γ point. As shown in Figure 4b, the excited state population decays at a moderately slower rate for the expanded lattice, depicting suppression of charge recombination and a longer carrier lifetime to some extent. The charge recombination time as included in Table 1 is evaluated by using the short

Table 1. Average Absolute Values of Nonadiabatic Coupling, Pure Dephasing Times, and Nonradiative Carrier Recombination Times in FAPbI₃ under Different Tensile Strains

tensile strain (kbar)	dephasing time (fs)	NA coupling (meV)	recombination time (ns)
0	3.92	1.8	6.3
2	3.88	1.4	8.1
5	4.12	2.0	7.2

time linear approximation of the exponential decay (see the Supporting Information for detail calculations). We find an electron–hole recombination time of 6.3 ns for pristine FAPbI₃. The nanosecond time scale for charge recombination is consistent with previous simulations and experimental studies exploring very similar hybrid perovskites.^{65–67} Under a tensile strain of 2 kbar, the FAPbI₃ lattice decreases the nonradiative decay rate and increases the recombination time to 8.1 ns, which is a relative enhancement of 33%. However, under further lattice expansion (i.e., 5 kbar), the recombination time has been calculated to be 7.2 ns, indicating a slightly increased recombination rate with respect to a smaller tensile strain.

The atomistic reason for the longer carrier recombination time can be understood by analyzing the influence of lattice expansion in terms of several factors such as the dephasing time, nonadiabatic electron–phonon coupling, and band gap fluctuation over time. The recombination rate varies inversely with the band gap and scales as the square of the nonadiabatic coupling strength according to Fermi’s golden rule.^{68,69} Larger structural and band gap fluctuations along the trajectory indicate enhanced electron–phonon nonadiabatic coupling due to the increased chances of VBM–CBM wave function mixing (see section S3). The dephasing time further influences the recombination rate by being added through the Franck–Condon factor. Physically, during nonradiative charge recombination, a pair of participating states form a coherence between them. Thus, quicker decoherence and weaker nonadiabatic coupling result in a longer recombination time.⁶⁹ As shown in Table 1, both nonadiabatic coupling and the dephasing time moderately decrease with the application of a 2 kbar tensile strain in the FAPbI₃ lattice. The localization of the VB (Figure 3) and the slight reduction in band gap fluctuation (Table S1) result in a weaker nonadiabatic coupling. These changes, along with a small increase in the average band gap (Table S1), collectively enhance the carrier lifetime of this halide perovskite under tensile strain as shown in Figure 4b. An increase in recombination time with lattice expansion agrees well with the several experimental reports.^{21,23} Note that with further increased tensile strain (i.e., 5 kbar) the recombination time decreases due to stronger nonadiabatic coupling and a longer decoherence time. An increase in structural dynamics (Figure 4a) and the number of band gap fluctuations (Table S1) enhance the nonadiabatic coupling, causing accelerated electron–hole recombination. However, a blue-shift in the band gap in this expanded lattice

partially suppresses the recombination, giving rise to a recombination time that is longer than that of the parent FAPbI₃. Details of the effects of tensile strain on electron–phonon coupling in FAPbI₃ are discussed in the [section S3](#).

In conclusion, our study elucidates the effect of lattice expansion on the structural and optoelectronic properties of FAPbI₃. Under tensile strain, the PbI framework is distorted with longer Pb–I bonds and less tilted PbI₆ octahedra. In the expanded lattice, the band gap increases and the valence band maxima decrease, influencing the charge carrier generation and their collection in the interface via modification of interfacial energies. By performing nonradiative charge carrier dynamics, we find that tensile strain slightly decreases the electron–hole recombination rate, indicating probable beneficial effects of lattice expansion on charge carrier dynamics in FAPbI₃. Our study suggests that one may fine-tune the lattice expansion to optimize the photovoltaics in these materials. Such precise control over lattice expansion can be achieved by compositional engineering where large A cations (GA and DMA) can partially substitute for FA in FAPbI₃. An alternative but more challenging approach can be fine-tuning the growth process during fabrication to incorporate residual tensile strain in the polycrystalline FAPbI₃ thin films. By demonstrating the complex relationship between lattice distortion and charge carrier dynamics in halide perovskites, our work provides guidelines for experimental studies to use tensile strain to control electronic functionalities and improve the performance of materials for photovoltaic applications.

METHODS

Density functional theory (DFT)-based simulations, as implemented in the Vienna Ab Initio Simulation Package (VASP), were performed for geometry relaxation and electronic structure calculations.^{70,71} The projected augmented-wave (PAW) method using a plane-wave basis set with an energy cut off of 520 eV was applied for all of the calculations.⁷² The exchange and correlation interactions were modeled using the generalized gradient approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE) functional form.⁷³ During geometry optimization of a 2 × 2 × 2 (eight FA cations) supercell, all interatomic forces were relaxed to <0.01 eV Å⁻¹, where a 4 × 4 × 4 Γ -centered Monkhorst–Pack⁷⁴ mesh was employed. Note that, as various studies have reported dynamic cation–PbI vibrational coupling in hybrid halide perovskites,^{60,75} we have applied the DFT-D3 method as suggested by Grimme⁷⁶ for all of our static and AIMD simulations. To simulate structural changes with tensile strain, the supercell was reoptimized under static expansive pressures up to a maximum 10 kbar. This range of tensile strains properly models the lattice expansion of the perovskite lattice as reported in several experimental studies (see the [Supporting Information](#) for details).^{19–23} For the electronic structures, the Brillouin zone integrations were performed in a Γ -centered 6 × 6 × 6 k -point mesh with Gaussian smearing of 0.01 eV. Spin–orbit coupling (SOC) and the Heyd–Scuseria–Ernzerhof screened hybrid functionals (HSE06) were further applied self-consistently to correct the electronic structure.⁷⁷ Hartree–Fock exchange of 43% was considered for the HSE06 functionals along with an empirical range separation parameter ω of 0.11 b⁻¹. Previous studies have shown that these computational parameters successfully model the near band edge electronic structure of hybrid halide perovskites.¹¹

To explore the charge carrier dynamics, the mixed quantum classical NAMD simulations were performed by employing the decoherence-induced surface hopping (DISH) technique.^{78,79} In this approach, the lighter electrons and heavier nuclei are treated as quantum mechanical and semiclassical objects, respectively. This method has been widely applied to simulate the excited state dynamics in inorganic and hybrid perovskites.^{80–83} *Ab initio* molecular dynamics simulations were performed with a plane-wave energy cutoff of 400 eV, a 3 × 3 × 3 Monkhorst–Pack k -point mesh, and a time step of 1 fs. The optimized structures under different tensile strains were heated to 300 K using repeated velocity rescaling for 4 ps. Following that, MD trajectories were simulated for an additional 4 ps in the microcanonical ensemble and considered further for the nonadiabatic coupling calculations. All of the 4000 geometries in the trajectories and 1000 stochastic realizations of the DISH process for each geometry were considered for computing electron–hole recombination using the PYXAID code.^{84,85} The pure dephasing time as formulated in the optical-response theory was considered for calculation of the decoherence time.⁸⁶ More details about these methods can be found in [section S3](#).

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: [10.1021/acs.jpclett.9b02020](https://doi.org/10.1021/acs.jpclett.9b02020).

Details of the FAPbI₃ structure in different phases, phase stability and change in structure under tensile strain, band alignment method, crystal orbital Hamilton population method, and details of charge carrier dynamics in FAPbI₃ under tensile strain ([PDF](#))

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Notes

The authors declare no competing financial interest.

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